

11. How many positive integers less than 1000 are relatively prime to 105? Two integers are relatively prime if their greatest common divisor is 1.
- A. 325    B. 457    C. 466    D. 533    E. 674
12. In isosceles  $\triangle ABE$  with base  $AB$ ,  $AB = 10$  and  $BE = 13$ . Square  $ABCD$  intersects  $\triangle ABE$  at points  $F$  and  $G$ . Find the area common to the interiors of the square and the triangle.
- A.  $125/3$     B. 35    C. 40    D.  $175/3$     E. 65
13. The equation  $x^{\log_{25} 9} + 9^{\log_{25} x} = 54$  has a solution in common with which of the following?
- A.  $x^3 - 125x^2 - x + 125 = 0$     B.  $x^3 + 5x^2 - 25x - 125 = 0$   
C.  $x^3 - 5x^2 - 25x + 125 = 0$     D.  $5x^3 + 5x^2 - 125x - 125 = 0$   
E.  $5x^3 - 5x^2 - 125x + 125 = 0$
14. If you have eight pairs of socks, each pair a different color, find the probability that if you randomly lose five socks, the remaining socks form exactly four matching pairs (and three unmatched socks).
- A.  $20/39$     B.  $7/13$     C.  $22/39$     D.  $23/39$     E.  $8/13$
15. If  $h(x) = 2x + 2$  and  $k(x) = 2x^3 - 7x^2 - 11x + 6$ , find the sum of all of the irrational zeros of  $h(k(x))$  and  $k(h(x))$ .
- A.  $1/2$     B.  $3/2$     C.  $7/2$     D.  $9/2$     E.  $11/2$
16. If  $h(x) = 2x + 2$  and  $k(x) = 2x^3 - 7x^2 - 11x + 6$ , find the sum of all of the rational zeros of  $h(k(x))$  and  $k(h(x))$ .
- A.  $-5/4$     B.  $-3/4$     C.  $-1/4$     D.  $1/4$     E.  $3/4$
17. In pentagon  $AMTYC$ ,  $AC = MT = 10$ ,  $YT = CY = 20$ ,  $\angle A = \angle M = 135^\circ$ , and  $\angle Y = 150^\circ$ . Find the area of the pentagon to the nearest square unit.
- A. 315    B. 318    C. 320    D. 323    E. 325
18. How many 4-digit numbers whose digits are all odd are multiples of 11?
- A. 80    B. 85    C. 90    D. 95    E. 100
19. Find the tens digit of  $3^{2007}$ .
- A. 0    B. 2    C. 4    D. 6    E. 8
20. In the sequence  $a_1, a_2, a_3, \dots$ ,  $a_1 = 1$ ,  $a_2 = 2$ ,  $a_3 = 5$ , and for all  $n \geq 3$ ,  $a_{n-1}a_{n-2} = 2a_n a_{n-2} - 2a_{n-1}a_{n-1}$ . Find  $a_{2006}/a_{2005}$ .
- A. 1002    B. 1002.5    C. 1003    D. 1003.5    E. 1004